### There Is No Largest Prime Number

Unfortunately

October 4, 2016



POLITÉCNICO DO PORTO

Alberto Simões albertosimoes@esmad.ipp.pt

# There Is No Largest Prime Number The proof uses reductio ad absurdum.



#### Theorem

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- 1. Suppose *p* were the largest prime number.
- 2. Let *q* be the product of the first *p* numbers.
- 3. Then q+1 is not divisible by any of them.
- 4. But q + 1 is greater than 1, thus divisible by some prime number not in the first p numbers.

## A longer title



- one
- ▶ two