## There Is No Largest Prime Number Unfortunately

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## Theorem

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## There Is No Largest Prime Number

 The proof uses reductio ad absurdum.
## P. PORTC)

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1. Suppose $p$ were the largest prime number.
2. Let $q$ be the product of the first $p$ numbers.
3. Then $q+1$ is not divisible by any of them.
4. But $q+1$ is greater than 1 , thus divisible by some prime number not in the first $p$ numbers.

## A longer title

- one
- two

